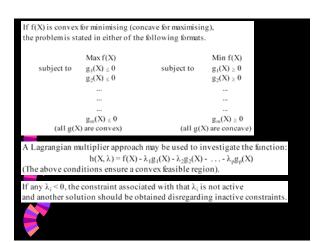
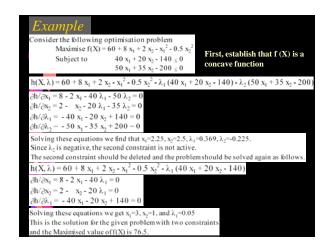


## Optimization of a Function of Multiple Variables subject to Inequality Constraints If there are only two variables, f(X) is analogous to the contour mapping of hill and g(X) are like several fences on the hill. The objective is to locate the point on the fences of that lies at the highest, or lowest elevation Convex Region: A region is convex, if a straight line connecting any two points in the region lies entirely in the region. If all constraints are straight lines, the feasible region will automatically be convex The procedures explained here are applicable only if the feasible region is convex. Otherwise search procedures are to be used





The Kuhn-Tucker Conditions are the necessary conditions for a point to be a local optimum of a function subject to inequality constraints. This is a precise mathematical statement of the procedure used in the previous section. Where  $X = [x_1 \ x_2 \ \dots \ x_n]$ , then  $Kuhn-Tucker Conditions for <math>X^* = [x_1^* \ x_2^* \ \dots \ x_n^*]$  to be a local optimum are  $\frac{\partial f(X)}{\partial x_i} - \sum_{j=1}^p \lambda_j \frac{\partial g_j(X)}{\partial x_i} = 0 \qquad for \ i=1,2,...,n \ at \ X=X^*$  and  $\lambda_j g_j(X) = 0 \qquad g_j(X) \le 0$   $\lambda_j \ge 0 \qquad for \ j=1,2,...,p \ at \ X=X^*$ 

Kuhn-Tucker Conditions

These are sufficient conditions for a global maximum if f(X) is concave and the constraints form a convex set