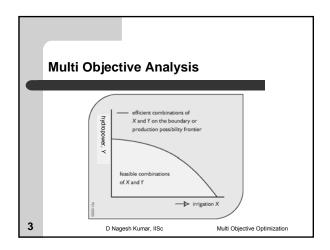
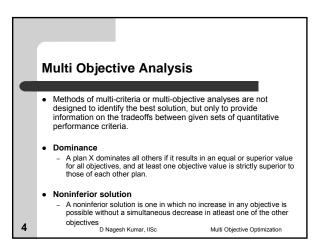
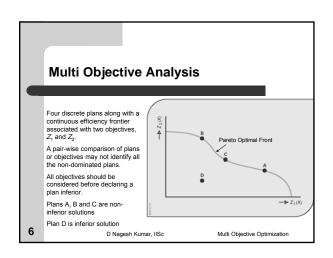


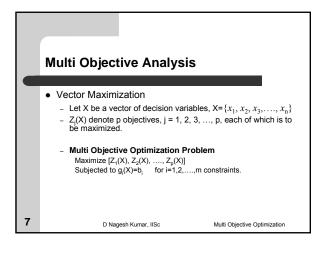
Multiple Objectives in Water Resources Maximizing aggregated net benefits is a common objective Other objectives include Water Quality, Regional Development, Resource Utilization, Social issues Conflicting objectives Irrigation, Hydropower, Recreation Multi objective optimization Trade-off analysis Multi Objective Optimization

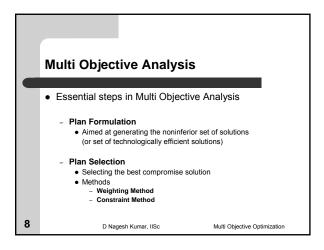




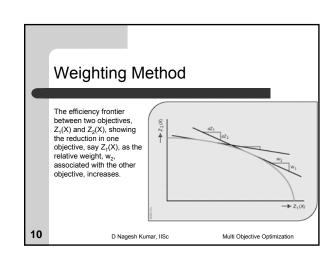
Non inferior, efficient, or non dminated solutions are often called Pareto optimal because they satisfy the conditions proposed by Italian economist Pareto, that to improve the value of any single objective, one should have to accept a diminishment of at least one other objective. | 5 | D Nagesh Kumar, IISC | Multi Objective Optimization | Multi Objective Opti

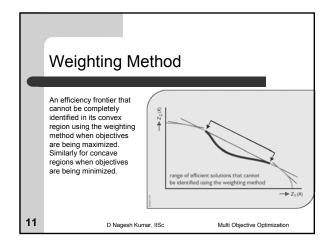


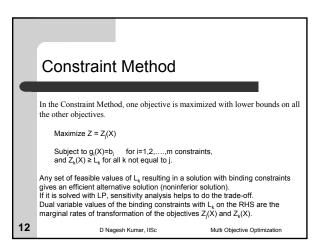


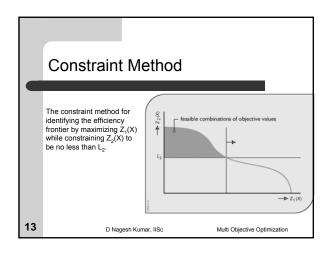


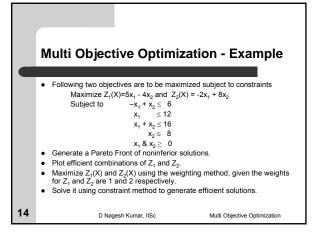
Weighting Method In the Weighting Method, the objective function (in the vector form) is converted to a scalar by expressing it as weighted sum of the various objectives by associating relative weight to each objective function. $Maximize\ Z = w_1\ Z_1(X) + w_2\ Z_2(X) + + w_p\ Z_p(X)$ Subject to $g_i(X) = b_i$ for i = 1, 2,, m constraints. Relative weights, w_p reflect the trade-off or the marginal rate of transformation of pairs of objective functions. Weights imply value judgments. These weights are varied systematically and solution is obtained for each set. Solution obtained for a set of weights gives one generated set of noninferior or efficient solutions are plans. Major limitation of weighting approach is that it cannot generate the complete set of efficient plans unless the Pareto front is strictly convex. Name of the vector form is plant of the vector form is strictly convex.

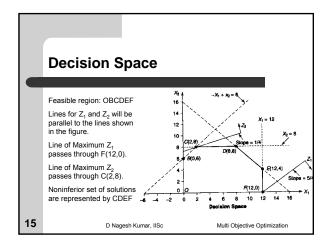


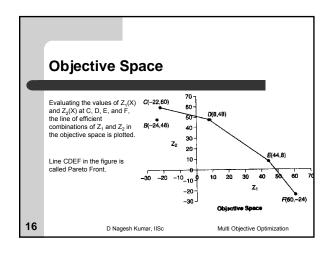


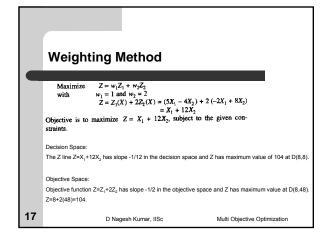


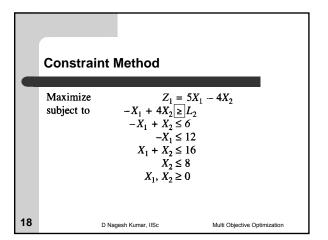












Methods for selecting the most desirable non-dominated plan

- Satisficing
- Lexicography
- Indifference Analysis
- Goal Attainment
- Goal Rogramming
- Interactive Methods
- Plan Simulation and Evaluation

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Multi Objective Optimization

Multi Objective Optimization Exercise Problem

 A reservoir is planned both for gravity and lift irrigation through withdrawals
from its storage. The total storage available for both the uses is limited to 5
units each year. It is decided to limit the gravity irrigation withdrawals in a
year to 4 units. If X, is the allocation of water to gravity irrigation and X₂ is
the allocation for lift irrigation, two objectives are planned to be maximized and are expressed as

Maximize $Z_1(X)=3x_1-2x_2$ and $Z_2(X)=-x_1+4x_2$

Generate a Pareto Front of noninferior solutions by plotting Decision space

Multi Objective Optimization

- Generate a Pareto Front or noninterior solutions by pioting Decision sparand Objective space.
 Formulate multi objective optimization model using weighting approach with w₁ and w₂ as weights for gravity and lift irrigation respectively.
 Solve it, if (i) w₁=1 and w₂=2 (ii) w₁=2 and w₂=1
 Formulate the problem using constraint method

Solution: (i) X₁=0, X₂=5; (ii) X₁=4, X₂=0 to 1;

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